Elliptic Problems in Smooth and in Non Smooth Domains

Chérif Amrouche Univeristé de Pau et des Pays de l'Adour, Pau, FRANCE cherif.amrouche@univ-pau.fr

 $23~\mathrm{mai}~2022$

We are interested here in questions related to the **maximal regularity** of solutions of **elliptic** problems with **Dirichlet** or **Neumann** boundary condition (see ([1]). For the last 40 years, many works have been concerned with questions when Ω is a **Lipschitz domain**. Some of them contain incorrect results that are corrected in the present work.

We give here new proofs and some complements for the case of the **Laplacian** (see [3]), the **Bilaplacian** ([2] and [6]) and the operator div $(A\nabla)$ (see ([5]), when **A** is a matrix or a function. And we extend this study to obtain other regularity results for domains having an adequate regularity. We give also new results for the **Dirichlet-to-Neumann** operator for Laplacian and Bilaplacian.

Using the duality method, we can then revisit the work of Lions-Magenes [4], concerning the so-called **very weak solutions**, when the data are less regular.

Acknowledgment : this is a joint work with Mohand Moussaoui (Ecole Normale Supérieure de Kouba, Alger, mmohand47@gmail.com)

Références

- C. Amrouche and M. Moussaoui. The Dirichlet and Neumann problems in Lipschitz and in C^{1,1} domains. Submitted.
- [2] B.E.J. Dahlberg, C.E. Kenig, J. Pipher and G.C. Verchota. Area integral estimates for higher order elliptic equations and systems. Ann. Inst. Fourier, 47-5, 1425–1461, (1997).
- [3] D. Jerison and C.E. Kenig. The Inhomogeneous Dirichlet Problem in Lipschitz Domains, J. Funct. Anal. 130, 161–219, (1995).
- [4] J.L. Lions and E. Magenes. Problèmes aux limites non-homogènes et applications, Vol. 1, Dunod, Paris, (1969).

- [5] J. Nečas. *Direct methods in the theory of elliptic equations*. Springer Monographs in Mathematics. Springer, Heidelberg, (2012).
- [6] G.C. Verchota. The biharmonic Neumann problem in Lipschitz domains. Acta Math. 194-2, 217–279, (2005).